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# Intersystem-crossing and excited-state absorption of C<sub>70</sub> studied by picosecond pump and probe absorption and fluorescence measurements

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## Abstract

The singlet and triplet absorption and emission dynamics of C<sub>70</sub> in toluene is studied with a picosecond Nd:glass laser double-pulse pump and probe transmission and fluorescence measurement technique. The singlet S<sub>1</sub> excited-state absorption ( $\sigma_{\text{ex,L}} \approx 6 \times 10^{-17} \text{ cm}^2$ ), the triplet T<sub>1</sub> absorption ( $\sigma_{\text{T}} \approx 4.2 \times 10^{-17} \text{ cm}^2$ ), and the triplet T<sub>2</sub> absorption ( $\sigma_{\text{ex,T}} \approx 4.3 \times 10^{-17} \text{ cm}^2$ ) at 527 nm are determined. The singlet to triplet intersystem-crossing is studied by double pump pulse induced fluorescence signal analysis and by double probe pulse transmission measurements. The yield of triplet formation is found to be near to unity. © 1998 Elsevier Science S.A. All rights reserved.

*Keywords:* Intersystem-crossing; Excited-state absorption; C<sub>70</sub>

## 1. Introduction

Since the discovery [1] and laboratory synthesis [2] of fullerenes their study is an active field of research [3]. The optical spectroscopy of C<sub>60</sub> and C<sub>70</sub> is reviewed in Refs. [3,4]. The ground-state absorption of C<sub>60</sub> [4–8] and C<sub>70</sub> [4,6–8] was analysed. Fluorescence studies of C<sub>60</sub> [9–12] and C<sub>70</sub> [9,11–15] have been performed. Small quantum yields of fluorescence ( $\phi_{\text{F}} \approx 2.2 \times 10^{-4}$  for C<sub>60</sub> [10], and  $\phi_{\text{F}} = 5.9 \times 10^{-4}$  [14] to  $8.5 \times 10^{-4}$  [9,16] for C<sub>70</sub>) were determined. The yield of triplet formation was found to be close to 100% (C<sub>60</sub>: [4,17]; C<sub>70</sub>: [4,18–21]). Triplet–triplet absorption spectra for C<sub>60</sub> and C<sub>70</sub> are presented in Refs. [4,19,20,22,23] and Refs. [4,20,21,23,24], respectively.

The excited-state absorption of C<sub>60</sub> [11,25–33] [34–40] and C<sub>70</sub> [11,15,24,26–28] has been studied mainly with respect to optical limiting applications (reverse saturable absorption) [28–32,34,35,38–41].

In this paper the singlet and triplet absorption and emission dynamics of C<sub>70</sub> in toluene at room temperature is investigated. The S<sub>1</sub>–S<sub>n</sub> ( $n > 2$ ) singlet–singlet, the T<sub>1</sub>–T<sub>l</sub> ( $l \geq 2$ ) and the T<sub>2</sub>–T<sub>m</sub> ( $m \geq 3$ ) triplet–triplet absorption cross-sections at 527 nm, and the quantum yield of triplet formation by S<sub>1</sub>–T<sub>1</sub> intersystem-crossing (population accumulation in T<sub>1</sub> state after intersystem-crossing) are determined.

Picosecond second-harmonic pulses of a mode-locked Nd:glass laser are used in the experiments. A double pump-pulse and double probe-pulse transmission [42] and a double pump pulse induced fluorescence measurement technique [43,44] are applied. Some absorption cross-sections and the quantum yield of triplet formation are deduced by comparing the experimental results with numerical simulations of the absorption and emission dynamics. The first picosecond pump pulse transmission depends on the S<sub>1</sub>–S<sub>n</sub> excited-state absorption dynamics (excited-state absorption cross-section,  $\sigma_{\text{ex,L}}$ , and S<sub>n</sub>-state relaxation time,  $\tau_{\text{ex}}$ ). The first probe pulse transmission is caused by the residual S<sub>0</sub>-ground-state absorption and the induced T<sub>1</sub>–T<sub>1</sub> triplet–triplet absorption at the time,  $t_{\text{D}}$ , of probe pulse passing. It depends on the yield of triplet formation,  $\phi_{\text{T}}$ , and the T<sub>1</sub> triplet absorption cross-section,  $\sigma_{\text{T}}$ . The second pump pulse transmission depends on the singlet–singlet and triplet–triplet absorption and relaxation dynamics. It allows to extract the higher excited-state T<sub>2</sub>–T<sub>m</sub> absorption cross-section,  $\sigma_{\text{ex,T}}$ . The second probe pulse transmission depends on the population accumulation in the T<sub>1</sub> triplet state. The second probe pulse transmission together with the first probe pulse transmission allows the separate determination of  $\sigma_{\text{T}}$  and  $\phi_{\text{T}}$ .

The first pump pulse induced fluorescence signal, S<sub>F,1</sub>, is determined by the pump pulse induced S<sub>1</sub>-state level population and the fluorescence quantum yield. The second pump pulse induced fluorescence signal, S<sub>F,2</sub>, is reduced compared to the first pump pulse induced fluorescence signal in the case

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of singlet–triplet intersystem-crossing since then the  $S_1$ -state level population is reduced. The ratio of  $S_{F,2}/S_{F,1}$  allows the determination of the quantum yield of triplet formation,  $\phi_T$  [43,44].

The  $S_1$ – $S_n$  excited-state absorption cross-section,  $\sigma_{ex,L}$ , and the  $T_1$ – $T_1$  absorption cross-section are found to be larger than the  $S_0$  ground-state absorption cross-section,  $\sigma_L$  (reverse saturable absorption [40]). The quantum yield of triplet formation,  $\sigma_T$ , by  $S_1$ – $T_1$  intersystem-crossing is determined to be close to 100%.

## 2. Experimental

The fullerene  $C_{70}$  was purchased from Aldrich ([5,6]-Fullerene  $C_{70}$ ) and is used without further purification. The solvent toluene is of analytical grade. The absorption cross-section spectrum,  $\sigma_a(\lambda)$ , of  $C_{70}$  in toluene at room temperature is displayed in Fig. 1 together with the fluorescence quantum distribution  $E_F(\lambda)$  (own measurements).

The double-pulse pump and probe transmission measurements have been carried out with a picosecond Nd:glass laser system [45]. The experimental arrangement is displayed in Fig. 2. The mode-locked laser generates a train of picosecond pulses. The time period of adjacent pulses is  $t_R = 10$  ns (resonator roundtrip time). Two adjacent pulses are separated from the pulse train by an electro-optic switch [47] and increased in energy by a Nd:phosphate glass laser amplifier. The pulses are frequency doubled in a CDA crystal [48] and the remaining fundamental light is filtered off (filter F1). The wavelength of the second-harmonic pump pulses is  $\lambda_L = 527$  nm. The pump pulse duration is  $\Delta t_L = 6$  ps. The second harmonic pump pulses are directed to the sample, S (cell thickness  $l = 1$  mm). They are increased in intensity by lens L1. The input peak energy density is determined by energy transmission measurement through rhodamine 6G in ethanol (saturable absorption [46]) with photodetectors PD1 and PD2. The energy transmission of the pump pulses is measured with the photodetectors PD1 and PD3 (small signal transmission  $T_0 = 0.0756 \pm 0.001$ ). The probe pulses are split-off from the pump pulses with a beam splitter and are attenuated with a filter (F2). They pass opposite to the pump pulse direction through the sample. Their temporal delay relative to the pump pulses is  $t_D = 9$  ns. The probe pulse diameter is adjusted by lens L2. The transmission of the probe pulses is registered with the detectors the PD1 and PD4.

The double-pump-pulse fluorescence measurements are carried out with the probe beam path covered. The fluorescence emitted in sideward direction is collected with lens, L3, and directed to the spectrometer, SP, with lens, L4. The fluorescence light in the spectral region from 640 to 840 nm is passed through the spectrometer and registered temporally resolved with a microchannel-plate photomultiplier (Hamamatsu type R1564U) and a fast digital oscilloscope (LeCroy type 9362, time resolution approximately 500 ps).

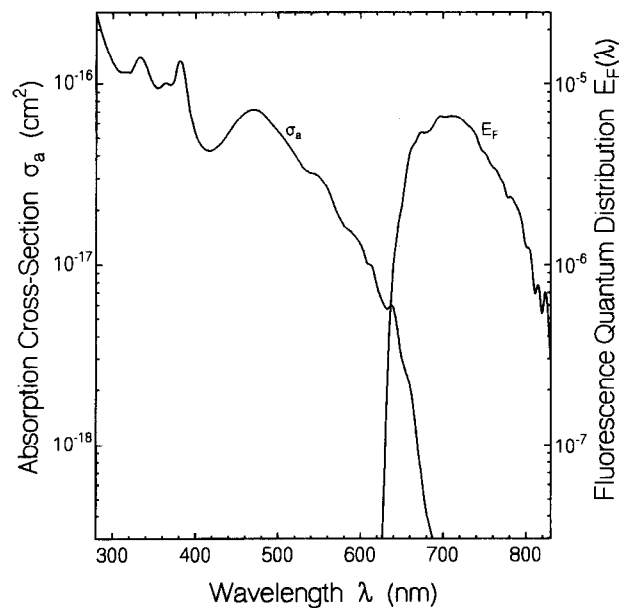


Fig. 1. Absorption cross-section spectrum,  $\sigma_a(\lambda)$ , and fluorescence quantum distribution,  $E_F(\lambda)$ , of  $C_{70}$  dissolved in toluene.

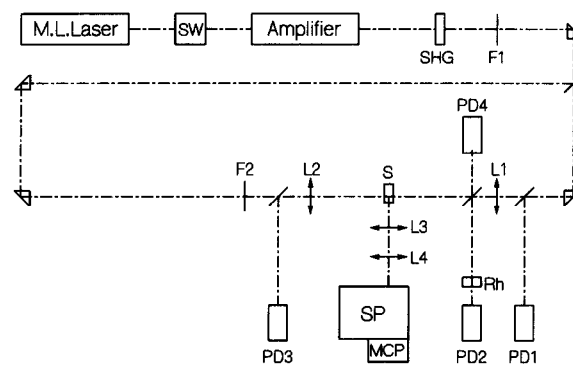


Fig. 2. Experimental setup. M.L. Laser, mode-locked Nd:glass laser. SW, single pulse selector. Amplifier, Nd:glass laser amplifier. SHG, frequency doubler. F1, cut-off filter of fundamental laser wavelength. L1–L4, lenses. Rh, rhodamine 6G in ethanol for energy density measurement [46]. PD1–PD4, photodetectors. S, sample. SP, spectrometer. MCP, microchannel-plate photomultiplier.

The intensity dependent transmission behaviour of the solvent toluene was measured separately with the experimental arrangement of Fig. 2 (pure toluene in sample cell, S). The measured energy transmission vs. input pump pulse peak intensity is displayed in Fig. 3. The transmission reduction at high pump pulse intensities is thought to be due to two-photon absorption [49]. The curves in Fig. 3 are calculated for various two-photon absorption coefficients,  $\alpha^{(2)}$ . The best fit is obtained for  $\alpha^{(2)} = (2 \pm 0.3) \times 10^{-10}$  cm/W. The two-photon absorption of the solvent is included in the analysis of the experimental results.

## 3. Experimental results

The pump pulse energy transmissions,  $T_{E,L1}$ ,  $T_{E,L2}$ , the probe pulse energy transmissions,  $T_{P1}$ ,  $T_{P2}$ , and the pump

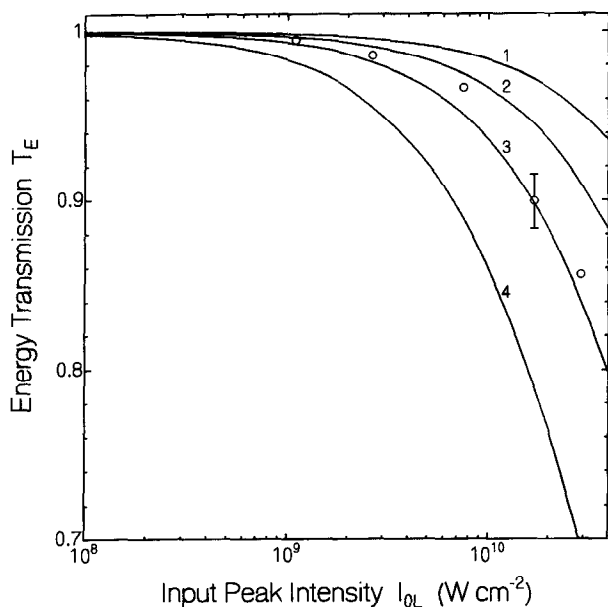


Fig. 3. Energy transmission through toluene. Pump laser wavelength,  $\lambda_L = 527$  nm. Sample length  $l = 1$  mm. Circles, experimental points. Curves are calculated for  $\alpha^{(2)} = 5 \times 10^{-11}$  cm/W (1),  $1 \times 10^{-10}$  cm/W (2),  $2 \times 10^{-10}$  cm/W (3), and  $5 \times 10^{-10}$  cm/W (4).

pulse induced fluorescence signal heights,  $S_{F,1}$ ,  $S_{F,2}$ , are measured as a function of the first pump pulse input peak intensity,  $I_{0L,1}$ . Data are selected where the second pump pulse peak intensity,  $I_{0L,2}$ , is approximately equal to the first pump pulse peak intensity. The probe pulse peak intensities are kept a factor of 250 smaller than the pump pulse peak intensities. The probe beam diameters were a factor of two narrower than the pump beam diameters at the sample position. The saturation intensity of  $S_0$  ground-state depopulation,  $I_{\text{sat}} = h\nu_L / (\sigma_L \Delta t_L)$  ( $h$ , Planck constant;  $\nu_L$ , second harmonic laser frequency;  $\sigma_L$  absorption cross-section at  $\nu_L$ ;  $\Delta t_L$ , duration of second harmonic pulses), is marked in Figs. (4)–(8) (slow saturable absorption conditions apply since  $\Delta t_L \ll \tau_{S_1}$ , where  $\tau_{S_1}$  is the  $S_1$ -state lifetime [50]).

The energy transmission,  $T_{E,L,1}$ , of the first pump pulse ( $\lambda_L = 527$  nm,  $\Delta t_L = 6$  ps) through  $C_{70}$  in toluene (small signal transmission  $T_0 = 0.0756$ ) is displayed by circles in Fig. 4. The transmission decreases with rising input pump pulse intensity. The behaviour indicates that the excited-state absorption is larger than the ground-state absorption at 527 nm (reverse saturable absorption).

The energy transmission,  $T_{E,L,2}$ , of the second pump pulse (time delay  $t_R = 10$  ns) through the sample is shown by circles in Fig. 5. The decrease in transmission with rising pump pulse intensity is similar to the behaviour of the first pulse. It indicates a larger  $T_1$ -triplet absorption than  $S_0$ -singlet absorption.

The first probe pulse transmission,  $T_{P,1}$  (time delay  $t_D = 9$  ns) is displayed by circles in Fig. 6. Its dependence is determined by the  $S_0$  ground-state absorption of the molecules, which have remained in the  $S_0$ -state, and by the  $T_1$ -triplet absorption of the molecules, which have proceeded to

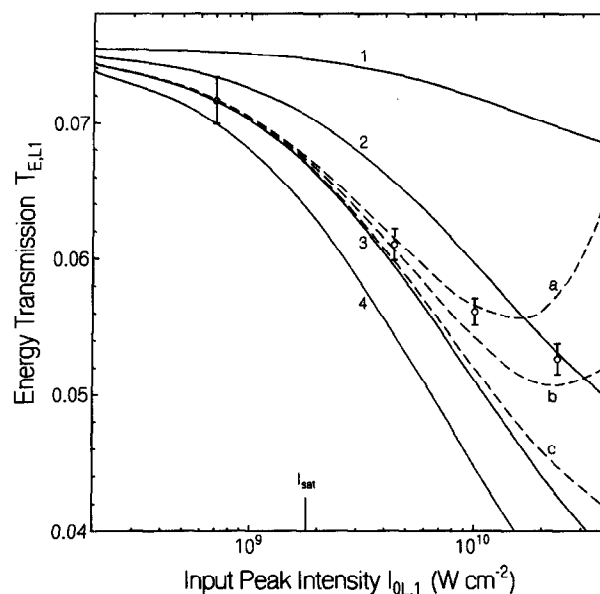


Fig. 4. Energy transmission,  $T_{E,L,1}$ , of first pump pulse through  $C_{70}$  in toluene vs. input pump pulse peak intensity,  $I_{0L,1}$ . Small signal transmission,  $T_0 = 0.0756$ . Circles are experimental data points. Curves are calculated using parameters of Table 1. Solid curves,  $\tau_{\text{ex}} = 60$  fs with  $\sigma_{\text{ex,L}} = 4 \times 10^{-17}$  cm $^2$  (1),  $5 \times 10^{-17}$  cm $^2$  (2),  $6 \times 10^{-17}$  cm $^2$  (3),  $7 \times 10^{-17}$  cm $^2$  (4). Dashed curves,  $\sigma_{\text{ex,L}} = 6 \times 10^{-17}$  cm $^2$  with  $\tau_{\text{ex}} = 300$  fs (a), 200 fs (b), 100 fs (c).

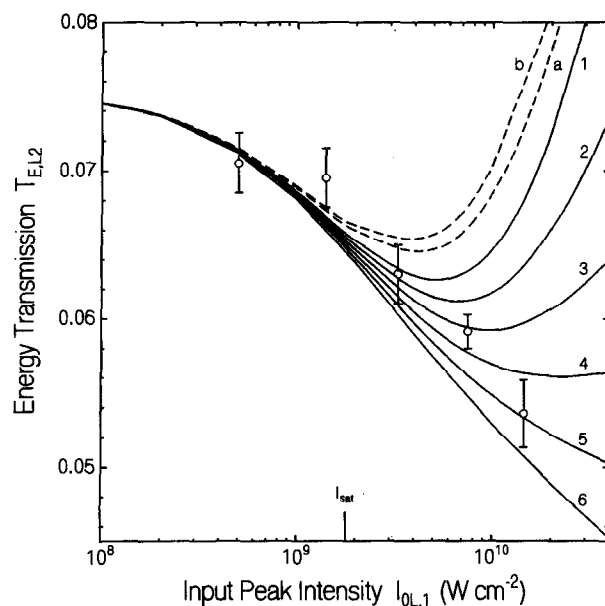


Fig. 5. Energy transmission of second pump pulse,  $T_{E,L,2}$ , vs. input peak intensity of first pump pulse (second pump pulse peak intensity is nearly the same as first pump pulse peak intensity). Circles are experimental data points. All curves are calculated for  $\sigma_T = 4.2 \times 10^{-17}$  cm $^2$ . Solid curves,  $\tau_T = 2$  ps and  $\sigma_{\text{ex,T}} = 2.5 \times 10^{-17}$  cm $^2$  (1),  $3 \times 10^{-17}$  cm $^2$  (2),  $3.5 \times 10^{-17}$  cm $^2$  (3),  $4 \times 10^{-17}$  cm $^2$  (4),  $4.5 \times 10^{-17}$  cm $^2$  (5), and  $5 \times 10^{-17}$  cm $^2$  (6). Dashed curves,  $\sigma_{\text{ex,T}} = 2.5 \times 10^{-17}$  cm $^2$  and  $\tau_T = 10$  ps (a), 100 ps (b). Other parameters are taken from Table 1.

the  $T_1$ -state. The probe pulse transmission reduces with rising first pump pulse peak intensity,  $I_{0L,1}$ . But the decrease in transmission of the first probe pulse is slightly smaller than the decrease of transmission of the first pump pulse indicating

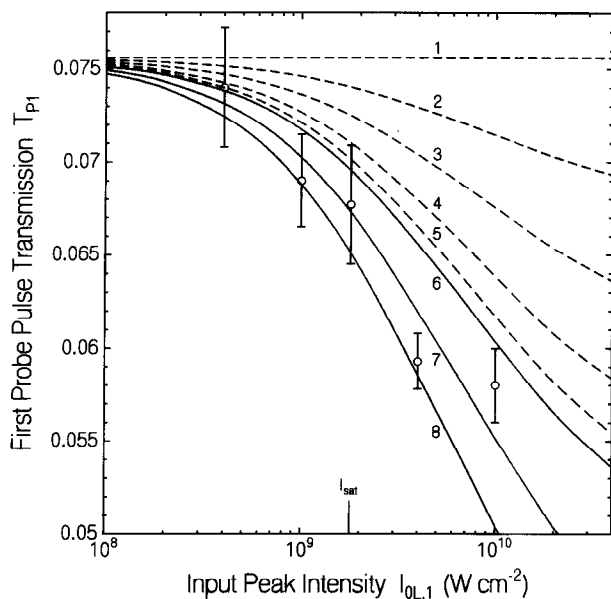


Fig. 6. Transmission of first probe pulse,  $T_{P1}$ , vs. first pump pulse peak intensity,  $I_{0L,1}$ . Circles are experimental results. The curves are calculated using the parameters of Table 1. Dashed curves,  $\sigma_T = 4 \times 10^{-17} \text{ cm}^2$  and  $\phi_T = 0$  (1), 0.25 (2), 0.5 (3), 0.75 (4), and 0.9 (5). Solid curves,  $\phi_T = 0.999$  and  $\sigma_T = 4 \times 10^{-17} \text{ cm}^2$  (6),  $4.2 \times 10^{-17} \text{ cm}^2$  (7), and  $4.4 \times 10^{-17} \text{ cm}^2$  (8).

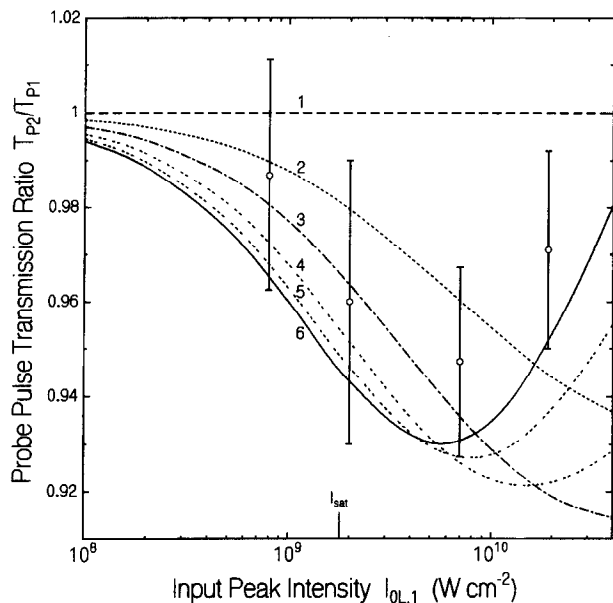


Fig. 7. Transmission ratio of probe pulses  $T_{P2}/T_{P1}$ , vs. input peak intensity of first pump pulse,  $I_{0L,1}$ . Circles are experimental data. Error bars show standard deviation of the mean transmission ratios. The curves are calculated for  $\phi_T = 0$  (1), 0.25 (2), 0.5 (3), 0.75 (4), 0.9 (5), 0.999 (6). Other parameters are taken from Table 1.

that the  $T_1$ -triplet absorption cross-section,  $\sigma_T$ , is smaller than the  $S_1$ -state excited-state absorption cross-section,  $\sigma_{ex,L}$ .

The ratio of second probe pulse transmission to first probe pulse transmission,  $T_{P2}/T_{P1}$ , is shown in Fig. 7. The transmission ratio is slightly less than one with a minimum around  $I_{0L,1} \approx 7 \times 10^9 \text{ W/cm}^2$ . The intensity dependent behaviour of  $T_{P1}$  and  $T_{P2}/T_{P1}$  is used below to extract  $\sigma_T$  and  $\phi_T$ .

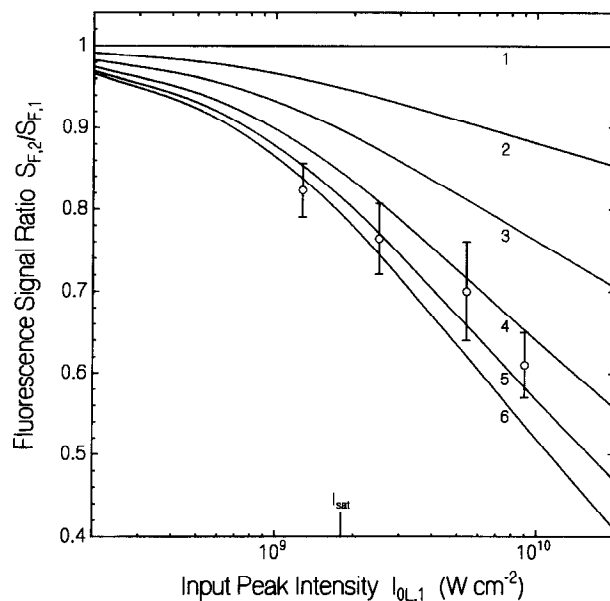


Fig. 8. Fluorescence signal ratio,  $S_{F,2}/S_{F,1}$ , vs. input peak intensity,  $I_{0L,1}$ . Circles are experimental data.  $T_0 = 0.0756$ . Differences in peak intensity of first and second pump pulse are corrected by  $S_{F,2}/S_{F,1} = (S_{F,2}/S_{F,1})_{\text{measured}} [I_{0L,1}/(1 + I_{0L,1}/I_{\text{sat}})] / [I_{0L,2}/(1 + I_{0L,2}/I_{\text{sat}})]$ . The curves are calculated for parameters of Table 1 and  $\phi_T = 0$  (1), 0.25 (2), 0.5 (3), 0.75 (4), 0.9 (5), and 0.999 (6).

The fluorescence signal ratio,  $S_{F,2}/S_{F,1}$ , of the second pump pulse induced peak fluorescence signal height to the first pump pulse induced peak fluorescence signal height is displayed in Fig. 8 (circles) as a function of the first pump pulse peak intensity,  $I_{0L,1}$ . The ratio decreases with increasing  $I_{0L,1}$ , indicating triplet level population by intersystem-crossing.

#### 4. Theoretical description

An extraction of the absorption cross-sections,  $\sigma_{ex,L}$ ,  $\sigma_T$ ,  $\sigma_{ex,T}$ , of the higher-excited-singlet-state relaxation time,  $\tau_{ex}$ , and of the  $S_1$ - $T_1$  intersystem-crossing rate,  $k_{35}$ , from the experimental transmission and fluorescence data requires a theoretical description of the absorption and emission dynamics and a numerical simulation of the experimental results.

The absorption dynamics of the two pump pulses and the two probe pulses is analysed using the energy level system of Fig. 9a and the double pump pulse and double probe pulse scheme of Fig. 9b. All pulses are linearly polarized in the same direction. The pump pulse induced fluorescence dynamics is determined by the dynamics of the  $S_1$ -level population.

##### 4.1. Level population and pulse propagation model

The first pump pulse excites molecules from the  $S_0$ -ground-state (level 1) to an excited singlet state (level 2; ground-state absorption cross-section,  $\sigma_L$ ). From there the molecules relax quickly (Franck–Condon relaxation time constant,  $\tau_{FC,S}$ ) to a thermal equilibrium position in the  $S_1$ -band (level

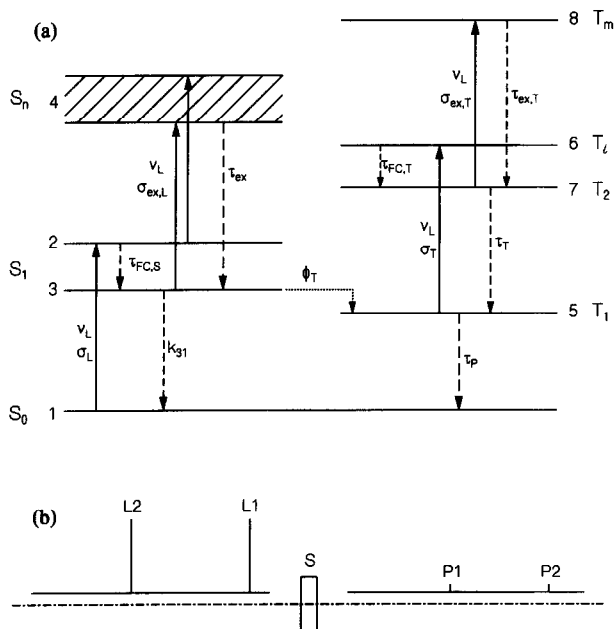


Fig. 9. (a) Energy level scheme for singlet-singlet absorption dynamics, triplet-triplet absorption dynamics, and  $S_1$ - $T_1$  singlet-triplet intersystem-crossing. (b) Scheme of double-pulse pump and double-pulse probe interaction in the sample.

3). From levels 2 and 3 there occurs  $S_1$ - $S_n$  excited-state absorption to band 4 (excited-state absorption cross-section,  $\sigma_{ex,L}$ ). The population in level 4 relaxes quickly to level 3 (relaxation time constant,  $\tau_{ex}$ ). The thermally relaxed  $S_1$ -state population (level 3) relaxes to the ground-state (relaxation rate constant,  $k_{31}$ ) and to the triplet system (intersystem-crossing rate constant,  $k_{35}$ ; yield of triplet formation,  $\phi_T$ ). The  $S_1$ -state lifetime,  $\tau_{S_1}$  (equal to the fluorescence lifetime,  $\tau_F$ ) is given by  $\tau_{S_1} = (k_{31} + k_{35})^{-1}$ . The  $S_1$ -state intersystem-crossing rate is  $k_{35} = \phi_T \tau_{S_1}^{-1}$ .

The first probe pulse, P1, passes through the sample after a time delay of  $t_{L1,P1} = t_D$  which is slightly shorter than the temporal pump pulse separation,  $t_R$ , but much longer than the  $S_1$ -state lifetime,  $\tau_{S_1}$ . The transmission,  $T_{P1}$ , of the probe pulse, P1, is given by the singlet ground-state absorption, which is determined by the  $S_0$ -ground-state population number density,  $N_1(t' = t_D)$ , and by the  $T_1$ -triplet absorption, which is determined by the population number density of the lowest triplet state,  $N_5(t' = t_D)$  ( $N_5(t' = t_D) = N_0 - N_1(t' = t_D)$ , where  $N_0$  is the total molecule number density).

The second pump pulse, L2, causes the same absorption and emission dynamics in the singlet system as the first pump pulse (but the initial ground-state population,  $N_1(t' = t_R)$ , is smaller) and additionally causes excitation and relaxation in the triplet system. The molecules in the triplet ground-state,  $T_1$  (level 5), are excited to a higher lying triplet state,  $T_l$  (level 6, triplet absorption cross-section,  $\sigma_T$ ). From there the molecules relax quickly to the lowest excited triplet state,  $T_2$  (Franck-Condon relaxation time constant,  $\tau_{FC,T}$ ). From the  $T_2$ -state (level 7) the molecules relax to the  $T_1$ -state with a time constant  $\tau_T$ . The back transfer from  $T_1$  to  $S_0$  occurs with

the phosphorescence lifetime,  $\tau_P$ , on a microsecond to millisecond time scale [16,18,20,21,51,52].

The second probe pulse passes through the sample after a time delay of  $t_{L1,P2} = t_R + t_D$  relative to the first pump pulse. Its transmission is determined by the  $S_0$  (level 1) and  $T_1$  (level 5) population number densities at the time of passing the sample.

Higher excited-state singlet  $\rightarrow$  triplet intersystem-crossing [53–56] and triplet  $\rightarrow$  singlet intersystem-crossing [42,57–60] are not included in the absorption and emission dynamics, since the transmission and fluorescence behaviour can be fitted reasonably well with the presented model and the error bars of the experimental data allow no further model refinement.

#### 4.2. Equation system

The saturable absorption dynamics of the two pump pulses and the two probe pulses is handled by the following differential equation system for the level population number densities,  $N_1$  to  $N_7$ , and the laser pulse intensities,  $I_{L1}$ ,  $I_{L2}$ ,  $I_{P1}$ , and  $I_{P2}$  [44]. Immediate relaxation from level 8 to level 7 is assumed ( $\tau_{ex,T} = 0$ ).

$$\frac{\partial N_1}{\partial t'} = -\sigma_L(N_1 - N_2) \frac{I_{L1} + I_{L2}}{h\nu_L} + k_{31}N_3 + \frac{N_5}{\tau_P} \quad (1)$$

$$\frac{\partial N_2}{\partial t'} = \sigma_L(N_1 - N_2) \frac{I_{L1} + I_{L2}}{h\nu_L} \quad (2)$$

$$-\sigma_{ex,L} \left( N_2 - \frac{N_2}{N_2 + N_3} N_4 \right) \frac{I_{L1} + I_{L2}}{h\nu_L} - \frac{N_2}{\tau_{FC,S}}$$

$$\frac{\partial N_3}{\partial t'} = \frac{N_2}{\tau_{FC,S}} - \sigma_{ex,L} \left( N_3 - \frac{N_3}{N_2 + N_3} N_4 \right) \frac{I_{L1} + I_{L2}}{h\nu_L} \quad (3)$$

$$+ \frac{N_4}{\tau_{ex}} - \frac{N_3}{\tau_{S_1}}$$

$$\frac{\partial N_4}{\partial t'} = \sigma_{ex,L} \left( N_2 + N_3 - N_4 \right) \frac{I_{L1} + I_{L2}}{h\nu_L} - \frac{N_4}{\tau_{ex}} \quad (4)$$

$$\frac{\partial N_5}{\partial t'} = \frac{\phi_T}{\tau_{S_1}} N_3 - \sigma_T \left( N_5 - N_6 \right) \frac{I_{L1} + I_{L2}}{h\nu_L} + \frac{N_7}{\tau_T} - \frac{N_5}{\tau_P} \quad (5)$$

$$\frac{\partial N_6}{\partial t'} = \sigma_T \left( N_5 - N_6 \right) \frac{I_{L1} + I_{L2}}{h\nu_L} - \frac{N_6}{\tau_{FC,T}} \quad (6)$$

$$\frac{\partial N_7}{\partial t'} = \frac{N_6}{\tau_{FC,T}} - \frac{N_7}{\tau_T} \quad (7)$$

$$\frac{\partial I_{Li}}{\partial z'} = - \left[ \sigma_L(N_1 - N_2) + \sigma_{ex,L}(N_2 + N_3 - N_4) + \sigma_T(N_5 - N_6) + \sigma_{ex,T}(N_7 + N_6) \right] I_{Li} - \alpha^{(2)} I_{Li}^2 \quad (8)$$

$$(i=1,2)$$

$$\frac{\partial I_{P_i}}{\partial z'} = -[\sigma_L N_1 + \sigma_T N_5] I_{P_i} \quad (i=1,2) \quad (9)$$

$$T_{E,i} = \frac{\int_0^\infty \int_{-\infty}^\infty r \int I_i(t', l, r) dt' dr}{\int_0^\infty \int_{-\infty}^\infty r \int I_i(t', 0, r) dt' dr} \quad (i=L1, L2, P1, P2) \quad (10)$$

The transformation  $t' = t - nz/c_0$  and  $z' = z$  is used, where  $t$  is the time,  $z$  is the distance along the propagation direction,  $c_0$  is the light velocity in vacuum, and  $n$  is the refractive index.  $l$  is the sample length. An absorption anisotropy is not considered since  $C_{70}$  is nearly spherical symmetric [3].

The initial conditions of the level populations are  $N_i(t' = -\infty, z', r) = N_0$  and  $N_i(t' = -\infty, z', r) = 0$  for  $i=2, \dots, 7$ .  $N_0$  is the total number density of dissolved fullerene molecules. The input pulse intensities are

$$I_{L1}(t', z' = 0, r) = I_{0L,1} \exp \left[ -\left(\frac{t'}{t_0}\right)^2 - \left(\frac{r}{r_L}\right)^2 \right] \quad (11)$$

$$I_{L2}(t', z' = 0, r) = I_{0L,2} \exp \left[ -\left(\frac{t' - t_R}{t_0}\right)^2 - \left(\frac{r}{r_L}\right)^2 \right] \quad (12)$$

$$I_{P1}(t', z' = 0, r) = I_{0P,1} \exp \left[ -\left(\frac{t' - t_D}{t_0}\right)^2 - \left(\frac{r}{r_P}\right)^2 \right] \quad (13)$$

$$I_{P2}(t', z' = 0, r) = I_{0P,2} \exp \left[ -\left(\frac{t' - t_D - t_R}{t_0}\right)^2 - \left(\frac{r}{r_P}\right)^2 \right] \quad (14)$$

$r$  is the radial beam coordinate.  $r_L$  and  $r_P$  are the  $1/e$  beam radii of the pump and the probe pulses, respectively.  $t_0 = 2^{-1} [\ln(2)]^{-1/2} \Delta t_L$  is half the  $1/e$  temporal pulse width ( $\Delta t_L$  is the FWHM pulse duration).

## 5. Data analysis

The equation system (1)–(10) is solved numerically using relevant parameters of  $C_{70}$  in toluene (see Table 1). Unknown parameters are determined by fitting the calculated energy transmissions of the pump and probe beams and the pump pulse induced fluorescence signals to the experimental values.

In Fig. 4 the first pump pulse energy transmission,  $T_{E,L1}$ , is simulated.  $T_{E,L1}$  depends on the  $S_1$ -excited-state absorption cross-section,  $\sigma_{ex,L}$ , and on the  $S_n$ -state relaxation time constant,  $\tau_{ex}$ . The solid curves are calculated for various  $\sigma_{ex,L}$ -values ( $\tau_{ex} = 60$  fs), while the dashed curves are calculated for different  $S_n$ -state relaxation times,  $\tau_{ex}$  ( $\sigma_{ex,L} = 6 \times 10^{-17}$  cm<sup>2</sup>). The best fit to the experimental data is obtained for  $\sigma_{ex,L} = 6 \times 10^{-17}$  cm<sup>2</sup> and  $\tau_{ex} = 240$  fs.

The double pump-pulse induced fluorescence signal behaviour is simulated in Fig. 8. The fluorescence signal ratio,  $S_{F,2}/S_{F,1}$ , depends on the yield of triplet formation,  $\phi_T$ .  $S_{F,2}/$

$S_{F,1}$  is practically independent of the explicit triplet–triplet absorption dynamics (verified by numerical simulation, but not shown in Fig. 8). The curves are calculated for various quantum yields of triplet formation,  $\phi_T$ . A comparison of the calculated curves with the experimental data gives  $\phi_T = 0.9 \pm 0.1$ . The experimental accuracy and subsequently the accuracy of  $\phi_T$  is limited to 10% because the fluorescence quantum yield,  $\phi_F$ , of  $C_{70}$  in toluene is very low ( $\phi_F \approx 8.5 \times 10^{-4}$ , see Table 1).

The first probe pulse transmission,  $T_{P1}$ , is simulated in Fig. 6.  $T_{P1}$  depends on the quantum yield of triplet formation,  $\phi_T$ , and on the cross-section,  $\sigma_T$ , of  $T_1 \rightarrow T_i$  triplet–triplet absorption. Knowing  $\phi_T$ , the fitting of calculated  $T_{P1}$  curves to experimental data allows the determination of  $\sigma_T$ . The dashed curves in Fig. 6 belong to various  $\phi_T$  values at a fixed value of  $\sigma_T = 4 \times 10^{-17}$  cm<sup>2</sup>. The solid curves are calculated for various  $\sigma_T$  values while the triplet quantum yield is fixed to  $\phi_T = 0.999$ . The best fit to the experimental data is obtained for  $\sigma_T = 4.2 \times 10^{-17}$  cm<sup>2</sup>.

The probe pulse transmission ratio,  $T_{P2}/T_{P1}$  is simulated in Fig. 7. The ratio depends on the yield of triplet formation,  $\phi_T$ , and the absorption cross-section ratio,  $\sigma_T/\sigma_L$ . If  $\sigma_T/\sigma_L = 1$  then the transmission ratio is  $T_{P2}/T_{P1} = 1$  independent of  $\phi_T$ . The combined dependence of  $T_{P1}$  (Fig. 6) and  $T_{P2}/T_{P1}$  on  $I_{0L,1}$  allows the determination of both  $\phi_T$  and  $\sigma_T$ . The best fit is obtained for  $\phi_T = 1 - \phi_F \approx 0.999$  and  $\sigma_T = 4.2 \times 10^{-17}$  cm<sup>2</sup>. A high accuracy of  $\sigma_T$  and  $\phi_T$  determination would be obtained, if  $\sigma_T$  were significantly different from  $\sigma_L$ . For  $C_{70}$  in toluene the singlet ground-state absorption cross-section,  $\sigma_L = 3.5 \times 10^{-17}$  cm<sup>2</sup>, and the  $T_1$  triplet-state absorption cross-section,  $\sigma_T = 4.2 \times 10^{-17}$  cm<sup>2</sup>, are only slightly different. Therefore the accuracy of  $\phi_T$  determination by  $T_{P1}$  and  $T_{P2}/T_{P1}$  measurement is moderate.

The second pump pulse transmission behaviour is simulated in Fig. 5.  $T_{E,L2}$  depends on the  $T_1 \rightarrow T_i$  triplet absorption,  $\sigma_T$ , on the  $T_2 \rightarrow T_m$  triplet excited-state absorption,  $\sigma_{ex,T}$ , and on the triplet–triplet relaxation time,  $\tau_T$ . Since  $\sigma_T$  has been already determined by probe pulse transmission measurements, the curves in Fig. 5 are calculated for various  $\sigma_{ex,T}$  values ( $\tau_T = 2$  ps, solid curves) and  $\tau_T$  values ( $\sigma_{ex,T} = 2.5 \times 10^{-17}$  cm<sup>2</sup>, dashed curves) to study their dependences. For  $\sigma_{ex,T}$  similar to  $\sigma_T$ , the second pump pulse transmission,  $T_{E,L2}$ , becomes practically independent of  $\tau_T$ . Our numerical fit gives  $\sigma_{ex,T} = (4.3 \pm 0.2) \times 10^{-17}$  cm<sup>2</sup>, while  $\sigma_T$  has been determined to be  $\sigma_T = (4.2 \pm 0.1) \times 10^{-17}$  cm<sup>2</sup>. Therefore, determination of  $\tau_T$  is not possible. In organic dyes typical values of  $\tau_T$  are of the order of 0.5 to 3 ps [42,44].

## 6. Discussion

The determined parameters,  $\sigma_L$ ,  $\sigma_{ex,L}$ ,  $\tau_{ex}$ ,  $\sigma_T$ ,  $\sigma_{ex,T}$ , and  $\phi_T$ , of  $C_{70}$  in toluene at room temperature for  $\lambda_L = 527$  nm are listed in Table 1 together with parameters reported in the literature.

Table 1  
Spectroscopic parameters of C<sub>70</sub> at room temperature

Parameter	Value	Comments
$\tau_{S_1}$ (ps)	110	[51]
	625	[9], undegassed
	627	[13], argon degassed benzene solution
	650	Used here
	660	[9], degassed
	670	[24]
	700	[27]
$\tau_F$ ( $\mu$ s)	0.710	[20], air saturated benzene solution
	0.730	[16], air saturated
	0.870	[18], air saturated benzene solution
	4–5	[18], argon-saturated
	41	[52], clusters in supersonic beam
	130	[16], degassed
	140	[21] in benzene
	53 000	[51], at 77 K in toluene/10% poly-( $\alpha$ -methylstyrene)
$\phi_F$	0.00059	[14]
	0.0007	[9], in benzene
	0.00085	[9,16] and own measurement, used here
$\phi_T$	0.76 $\pm$ 0.15	[21], in benzene
	0.9	[19]
	0.99 $\pm$ 0.02	[18]
	1 $\pm$ 0.15	[20], in benzene and hexane
	1 ( $\geq$ 0.85)	This work
$\tau_{FC,S}$ (ps)	0.5	Assumed [61], used here
$\tau_{FC,T}$ (ps)	0.5	Assumed, used here
$\tau_{ex}$ (fs)	240 $\pm$ 40	This work
$\tau_T$ (ps)	2	Assumed [42,44]
$\sigma_L$ (cm <sup>2</sup> )	3.2 $\times$ 10 <sup>-17</sup>	[21], in benzene
	3.5 $\times$ 10 <sup>-17</sup>	Own measurement, used here
$k_{35}$ (s <sup>-1</sup> )	1.25 $\times$ 10 <sup>9</sup>	[15], in benzene
	1.54 $\times$ 10 <sup>9</sup>	$k_{53} = \phi_T \tau_{S_1}^{-1}$ , used here
$\sigma_T$ (cm <sup>2</sup> )	3.6 $\times$ 10 <sup>-17</sup>	[23], in benzene
	3.8 $\times$ 10 <sup>-17</sup>	[21], in benzene
	3.9 $\times$ 10 <sup>-17</sup>	[20], in hexane
	(4.2 $\pm$ 0.1) $\times$ 10 <sup>-17</sup>	This work
	4.75 $\times$ 10 <sup>-17</sup>	[20], in benzene
$\sigma_{ex,L}$ (cm <sup>2</sup> )	(6.0 $\pm$ 0.5) $\times$ 10 <sup>-17</sup>	This work
$\sigma_{ex,T}$ (cm <sup>2</sup> )	(4.3 $\pm$ 0.2) $\times$ 10 <sup>-17</sup>	This work

Solvent toluene except stated otherwise.

The ratio of singlet excited-state absorption to singlet ground-state absorption is  $\sigma_{ex,L}/\sigma_L \approx 1.7$ . The S<sub>1</sub> state lifetime is  $\tau_{S_1} \approx 650$  ps. For picosecond pulses (pulse duration,  $\Delta t_L$ , less than S<sub>1</sub>-state lifetime,  $\tau_{S_1}$ ), C<sub>70</sub> in toluene behaves as a reverse saturable absorber since  $\sigma_{ex,L} > \sigma_L$ . On a nanosecond time scale (pulse duration or time of observation longer than  $\tau_{S_1}$ ) the nonlinear transmission behaviour is determined by  $\sigma_T/\sigma_L$ . For C<sub>70</sub> in toluene this absorption cross-section ratio is  $\sigma_T/\sigma_L \approx 1.2$  and the reverse saturable absorption effect is rather weak.

Our double-pulse fluorescence measurements and probe pulse transmission measurements agree well with a quantum yield of triplet formation of  $\phi_T \approx 1 - \phi_F$  ( $\phi_F \approx 8.5 \times 10^{-4}$ ). Triplet quantum yields close to 100% have been reported by several groups (see Table 1). The S<sub>1</sub>-state relaxation of C<sub>70</sub>

(as well as of C<sub>60</sub> [4,17]) is dominated by intersystem-crossing. The rate of internal conversion is small compared to the rate of intersystem-crossing (because  $\phi_T$  close to 1). The radiative relaxation time constant is long compared to the time constant of intersystem-crossing,  $\tau_{isc}$  ( $\tau_{isc} = k_{35}^{-1} = \phi_T \tau_{S_1} \approx 650$  ps;  $\tau_{rad} \approx \tau_{S_1} / \phi_F \approx 760$  ns).

A higher-excited-state relaxation time of  $\tau_{ex} = (240 \pm 40)$  fs has been determined for C<sub>70</sub> in toluene. In organic dyes the higher-excited-state S<sub>n</sub>  $\rightarrow$  S<sub>1</sub> singlet relaxation is generally fast in the 50 to 100 fs time range [62,63]. Only in the case of large energy gaps between S<sub>2</sub> and S<sub>1</sub> longer relaxation times are expected [64] and observed [65,66]. The symmetry of the C<sub>70</sub> molecule and its weak S<sub>0</sub>-S<sub>1</sub> absorption cross-section may be responsible for the moderate S<sub>n</sub>  $\rightarrow$  S<sub>1</sub> relaxation time constant,  $\tau_{ex}$ , of C<sub>70</sub>.

## 7. Conclusions

The singlet and triplet absorption dynamics of C<sub>70</sub> in toluene at room temperature has been studied with picosecond pulses at 527 nm. A double pump pulse induced fluorescence signal technique and a double pump pulse induced probe pulse transmission technique have been employed to determine the yield of triplet formation. Despite the fact of low fluorescence quantum yield and only slight difference between singlet ground-state and lowest-triplet absorption cross-sections, the quantum yield of triplet formation could be determined by both methods (fluorescence technique and absorption technique). The S<sub>1</sub>–S<sub>n</sub> excited-state absorption-cross-section, the S<sub>n</sub>-state relaxation time, as well as the T<sub>1</sub>–T<sub>l</sub> and T<sub>2</sub>–T<sub>m</sub> absorption cross-sections have been determined.

The presented methods of double pump pulse induced fluorescence detection and double pump pulse induced probe pulse transmission measurement may be generally applied to the determination of quantum yields of triplet formation. The presented pump and probe pulse transmission analysis generally allows the extraction of excited-state absorption cross-section and excited-state relaxation parameters.

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